

Time resource management of OAR based on fuzzy logic priority for multiple target tracking

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Abstract: For coping with the multiple target tracking in the presence of complex time-varying environments and unknown target information, a time resource management scheme based on chance-constraint programming (CCP) employing fuzzy logic priority is proposed for opportunistic array radar (OAR). In this scheme, the total beam illuminating time is minimized by effective time resource allocation so that the desired tracking performance is achieved. Meanwhile, owing to the randomness of radar cross section (RCS), the CCP is used to balance tracking accuracy and time resource conditioned on the specified confidence level. The adaptive fuzzy logic prioritization, imitating the human decision-making process for ranking radar targets, can realize the full potential of radar. The Bayesian Cramér-Rao lower bound (BCRLB) provides us with a low bound of localization estimation root-mean-square error (RMSE), and equally important, it can be calculated predictively. Consequently, it is employed as an optimization criterion for the time resource allocation scheme. The stochastic simulation is integrated into the genetic algorithm (GA) to compose a hybrid intelligent optimization algorithm to solve the CCP optimization problem. The simulation results show that the time resource is saved strikingly and the radar performance is also improved.

Keywords: chance-constraint programming (CCP), fuzzy logic priority, opportunistic array radar (OAR), root-mean-square error (RMSE), Bayesian Cramér-Rao lower bound (BCRLB).

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1. Introduction

Opportunistic array radar (OAR) proposed by the United States Naval Postgraduate School (NPS) is a new system radar for next generation naval stealth destroyer DD(X) [1–3]. In OAR, the stealth of the military platform is taken as the core and the digital array is regarded as the base, and then the array elements and the transmit/receive (T/R) modules are placed arbitrarily and aperiodically at available open areas over the entire 3-D space of the platform

[4,5]. Due to the unique structure of the antenna array of OAR, we can realize that parts of the array elements are in activation state while the others are shut down. Hence, multiple orthogonal beams can be generated simultaneously with various desired beam patterns [6,7]. However, in the most stressing conditions, the targets are so many that there are insufficient beams to track all the targets, and the competition for limited beam resources onboard the military platform remains unabated. Therefore, the conflicts between targets have to be resolved when the radar system operates in an environment that leads to an overload situation.

The time resource management is a rational allocation of dwell time over all the targets, or can be called beam dwell scheduling policy [8,9]. Generally speaking, two kinds of time resource management policies are considered. In the first policy, an optimal time resource allocation is selected so that the achievable localization root-mean-square error (RMSE) is minimized; in the second policy, the total illuminating time used for the estimation process is minimized for the desired tracking accuracy threshold [10]. However, when the radar systems are installed on the mobile platforms operating over prolonged time periods with limited resources, we merely need to obtain a desired performance level instead of minimizing the tracking error as much as possible [11], i.e., the latter type might be more useful in practical work.

In the traditional study of radar resource management, the radar cross section (RCS) is taken as a determined value at every instant while the targets are illuminated [11,12]. In practical target tracking process, attributing to the significantly variable environment and the ambiguous target information, the target RCS is uncertain [13], i.e., the RCS is a random variable. Therefore, we introduce chance-constraint programming (CCP) [14] to achieve a trade-off between time resource and tracking accuracy. Through this CCP, the total tracking accuracy could be attained under a certain confidence level so that the time resource for tracking would be reduced more.

When the aforementioned time resource CCP model is

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built, the priority of the targets is different. In the previous study, the fixed prioritization method for ranking targets is applied in the proposed resource management policies [15,16], or the nonrepresentational concepts [17], such as importance, urgency and validity, are attached to the radar targets instead of considering the concrete concepts, for instance, velocity, range, azimuth and height, etc. These methodologies cannot intelligently determine the priority of radar targets by a clear concept. Nevertheless, the fuzzy logic adaptive prioritization approach is an intelligent and effective method to calculate the priority of radar targets [18–20]. Considering the dynamic characteristics of target tracking, the fuzzy logic adaptive prioritization approach can imitate the human decision-making process and provide an intelligent and efficient algorithm to rank the targets.

Besides the above preparation, we also need to find a variable as the measurement criteria of the tracking accuracy of radar targets for pre-allocating time resources. And this problem has been addressed in published references of resource management [21–26]. The recursive Bayesian Cramér-Rao lower bound (BCRLB) was first derived in [21], where an elegant method is provided for computing Bayesian information matrix (BIM) avoiding manipulating large matrices. An upgraded derivation which is applicable to the nonlinear dynamics process is contained in [22], and the contributions of the prior information matrix and the data information matrix are separated by this derivation. The BCRLB is widely applied to the resource management of radar system by the simplified computing method, and excellent results are obtained [23–26].

On the basis of the aforementioned study, in this paper, we propose a time resource management scheme based on CCP with multibeam working mode employing fuzzy logic priority for tracking multiple, broadly distributed and independent point targets. It is assumed that only one target is in the region illuminated by a beam at every instant, however, a beam can successively track multiple targets in every frame. Though the aim is to minimize the total illuminating time of all the beams conditioned on the specified tracking performance threshold, the total illuminating time of one beam can be minimized by rational combinatorial optimization of radar targets among the beams. Meanwhile, the fuzzy if-then inference rules are invited to calculate the fuzzy logic priority of radar targets, and the number of fuzzy rules required to assess the value of influence factors plays an important role in guaranteeing the veracity and smoothness of the prioritization curves. The whole algorithm can be viewed as an intelligent response of radar systems to multiple target tracking by perceiving the environments. The BCRLB, measuring the estimated RMSE of target tracking accuracy, provides us a criterion for pre-allocating the time resource. By integrating stochastic

simulation and the genetic algorithm (GA), the optimal solutions can be derived.

This paper is organized as follows. The system model is introduced in Section 2. In Section 3, the random CCP model combining fuzzy logic inference system is formulated. Section 4 proposes an approach for solving the model. Several numerical results are provided in Section 5. Finally, the conclusions and future work of this paper are given in Section 6.

2. System model

We consider 2-dimensional multiple target tracking employing a colocated OAR, located at (x_0, y_0) . This system adopts a multibeam concept in which multiple simultaneous and independent beams are synthesized by different probing signals from various colocated transmitters. Hence, the OAR can generate M orthogonal transmit beams simultaneously. One beam can only cover one target at every instant. Let T_0 denote the time interval of successive frames, which is regarded as the tracking sample interval. Then the q th ($q = 1, 2, \dots, Q$ and $Q \geq M$) target at time kT_0 is located at (x_k^q, y_k^q) ($k = 0, 1, 2, \dots, K$), and moves at the speed of $(\dot{x}_k^q, \dot{y}_k^q)$. The multiple target tracking sketch is shown in Fig. 1.

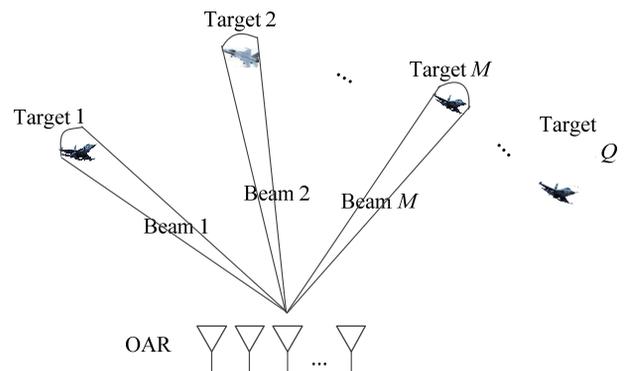


Fig. 1 Multiple target tracking sketch of OAR

2.1 Signal model

It is assumed that the transmitting signal of OAR to the q th target at the k th sample interval is

$$s_k^q(t) = \sqrt{p_k^q} S_k^q(t) \exp(-j2\pi f_c t) \quad (1)$$

where p_k^q denotes the transmitting power to the q th target at the k th sample interval, and f_c is the carrier frequency. $S_k^q(t)$ denotes the complex envelope of the transmitting signal, and its effective bandwidth [27] is

$$(B_k^q)^2 = \frac{\int_{-\infty}^{+\infty} (f - \bar{f})^2 |S_k^q(f)|^2 df}{\int_{-\infty}^{+\infty} |S_k^q(f)|^2 df} \quad (2)$$

where \bar{f} represents the first order origin moment of frequency spectrum $|S_k^q(f)|^2$, and in general, $\bar{f} = 0$. The effective time duration of $S_k^q(t)$ [27] is

$$(T_k^q)^2 = \frac{\int_{-\infty}^{+\infty} (t - \bar{t})^2 |S_k^q(t)|^2 dt}{\int_{-\infty}^{+\infty} |S_k^q(t)|^2 dt} \quad (3)$$

where \bar{t} represents the first order origin moment of $|S_k^q(t)|^2$, and in general, $\bar{t} = 0$. The effective time duration T_k^q of each target is impacted by the illuminating time of the corresponding beam, which is allocated rationally and optimally over all the targets.

The baseband representation for the echo signal from the q th target at the k th sample interval is

$$r_k^q(t) = h_k^q \sqrt{\alpha_k^q p_k^q} S_k^q(t - \tau_k^q) \cdot \exp(-j2\pi f_k^q t) + w_k^q(t) \quad (4)$$

where h_k^q denotes the target RCS, which is a random variable [13]. $\alpha_k^q \propto 1/(R_k^q)^4$ denotes the variation in the signal strength due to the path loss effect along the path OAR-target q -OAR. The time delay is τ_k^q and the Doppler frequency is f_k^q . $w_k^q(t)$ is a zero-mean, complex Gaussian white noise.

2.2 Motion model

The q th target moves rectilinearly with a constant velocity in the xy plane:

$$\xi_k^q = \mathbf{F}_q \xi_{k-1}^q + \mathbf{v}_{k-1}^q \quad (5)$$

where $\xi_k^q = [x_k^q \ \dot{x}_k^q \ y_k^q \ \dot{y}_k^q]^T$ denotes the state vector of the q th target at the k th sample interval. \mathbf{F}_q is the 4×4 transition matrix:

$$\mathbf{F}_q = \begin{bmatrix} 1 & T_0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & T_0 \\ 0 & 0 & 0 & 1 \end{bmatrix}. \quad (6)$$

\mathbf{v}_{k-1}^q represents a zero-mean, complex Gaussian white noise, and its covariance is

$$\mathbf{Q}_{k-1}^q = I_q \begin{bmatrix} \frac{1}{3}T_0^3 & \frac{1}{2}T_0^2 & 0 & 0 \\ \frac{1}{2}T_0^2 & T_0 & 0 & 0 \\ 0 & 0 & \frac{1}{3}T_0^3 & \frac{1}{2}T_0^2 \\ 0 & 0 & \frac{1}{2}T_0^2 & T_0 \end{bmatrix} \quad (7)$$

where I_q is the process noise intensity of the q th target [27].

2.3 Measurement model

The received signal from the q th target is an attenuated version of the transmitted signal. The range, azimuth and Doppler frequency can be extracted from the received signal. The nonlinear measurement equation can be written as

$$\mathbf{z}_k^q = \mathbf{g}(\xi_k^q) + \mathbf{w}_k^q \quad (8)$$

where

$$\mathbf{g}(\xi_k^q) = (R_k^q, \theta_k^q, f_k^q)^T. \quad (9)$$

R_k^q denotes the range between the OAR and the q th target, and it can be calculated by the time delay τ_k^q .

$$R_k^q = \frac{c\tau_k^q}{2} = \sqrt{(x_k^q - x_0)^2 + (y_k^q - y_0)^2} \quad (10)$$

where c is the light speed. The azimuth θ_k^q can be expressed as

$$\theta_k^q = \arctan[(y_k^q - y_0)/(x_k^q - x_0)]. \quad (11)$$

f_k^q is the Doppler shift determined by the target coordinates and the velocity:

$$f_k^q = -\frac{2}{\lambda_k^q} (\dot{x}_k^q, \dot{y}_k^q) \cdot (x_k^q, y_k^q)^T / R_k^q \quad (12)$$

where $(\cdot)^T$ denotes matrix transposition, and λ_k^q denotes the wavelength.

\mathbf{w}_k^q is a zero-mean and Gaussian white noise, and its covariance is

$$\mathbf{R}_{\xi_k^q} = \text{blkdiag}(\sigma_{R_k^q}^2, \sigma_{\theta_k^q}^2, \sigma_{f_k^q}^2) \quad (13)$$

where $\text{blkdiag}(\cdot)$ denotes block diagonal matrix. $\sigma_{R_k^q}^2, \sigma_{\theta_k^q}^2$ and $\sigma_{f_k^q}^2$ are the BCRLB of MSE of the range, azimuth and Doppler shift at high signal-to-noise ratio (SNR). The BCRLB for $\sigma_{R_k^q}^2$ and $\sigma_{f_k^q}^2$ are given in Chapter 10 of [27] and the BCRLB for $\sigma_{\theta_k^q}^2$ follows from [28]. The number of coherent pulses illuminating the q th target is L_k^q , and T_1 is the effective time duration of a signal coherent pulse. Then the BCRLB of MSE of the range, azimuth and Doppler shift can be described as follows:

$$\begin{cases} \sigma_{R_k^q}^2 \propto (L_k^q (S/N)_k^q \cdot (B_k^q)^2)^{-1} \\ \sigma_{\theta_k^q}^2 \propto (L_k^q (S/N)_k^q / (B_{NN})^2)^{-1} \\ \sigma_{f_k^q}^2 \propto (L_k^q (S/N)_k^q \cdot (L_k^q \cdot T_1)^2)^{-1} \end{cases} \quad (14)$$

where B_{NN} is the null-to-null beamwidth of the receiver antenna. $(S/N)_k^q$ is the SNR of the echo signal of a single coherent pulse from the q th target at the k th sample interval:

$$(S/N)_k^q \propto \alpha_k^q |h_k^q|^2 p_k^q. \quad (15)$$

Hence, the measurement equation can be transformed as follows:

$$\mathbf{z}_k^q = (\tilde{R}_k^q, \tilde{\theta}_k^q, \tilde{f}_k^q)^T =$$

$$(R_k^q, \theta_k^q, f_k^q)^T + (\Delta R_k^q, \Delta \theta_k^q, \Delta f_k^q)^T \quad (16)$$

where ΔR_k^q , $\Delta \theta_k^q$ and Δf_k^q are the error information of the range, azimuth and Doppler shift, respectively.

2.4 Fuzzy logic adaptive prioritization

By other sensors, other operating modes or a tracking algorithm of OAR, we can obtain the information for assigning priority of tracked targets. On the basis of the information, the fuzzy logic adaptive prioritization method can calculate the priority of tracked targets intelligently as the human decision-making process.

2.4.1 Fuzzy values of fuzzy variables

The decision tree [19,20] is used for evaluating the priority of tracked targets. The influence factors of the priority contain the range, velocity, height, azimuth, range rate, identity, manoeuvre and weapon system, etc. In order to simplify the calculation, three different fuzzy variables providing information concerning the priority are considered: range, velocity and threat. ‘Threat’ is the fuzzy variable which represents the degree of threat of a target according to its trajectory and identity. The exactness of priority is proportional to the number of fuzzy values of each fuzzy variable. We attribute seven fuzzy values, three fuzzy values, three fuzzy values and seven fuzzy values to the fuzzy variables ‘range’, ‘velocity’, ‘threat’ and ‘priority’, respectively. The detailed definition of fuzzy values are listed in Table 1 [19, 20].

Table 1 Fuzzy values related to fuzzy variables

Fuzzy variable	Fuzzy value
Range	Very close, close, medium-close, medium, medium-far, far, very far
Velocity	Slow, medium, fast
Threat	Low, medium, high
Priority	Very low, low, medium-low, medium, medium-high, high, very high

The four fuzzy variables change within their respective domains: ‘range’ changes within 0–150 km; ‘velocity’ changes within 0–900 m/s; ‘threat’ and ‘priority’ both change within 0–1. The triangular fuzzy number is used to represent the membership function of fuzzy values of fuzzy variables. The membership functions, which are employed for the fuzzy values of ‘range’, ‘velocity’, ‘threat’ and ‘priority’, are presented in Fig. 2.

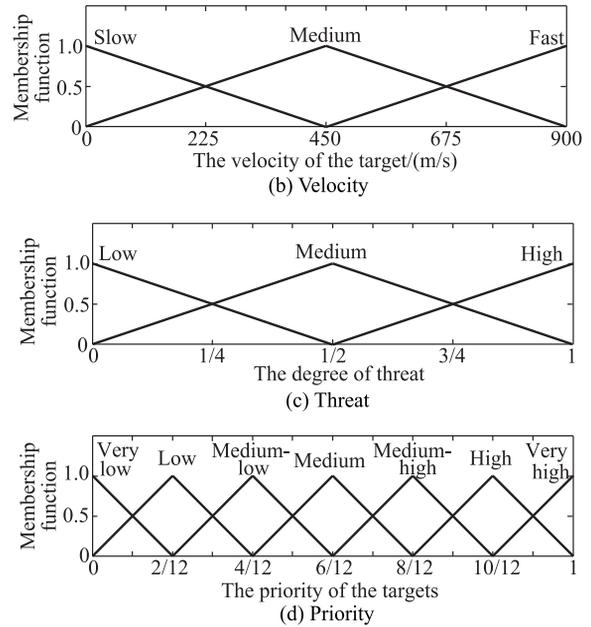
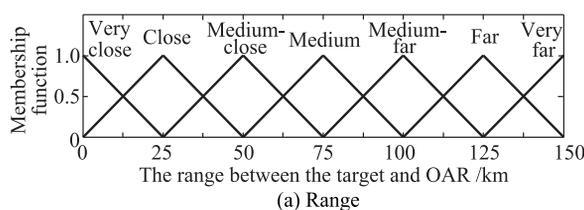


Fig. 2 Membership function related to fuzzy variables

2.4.2 Fuzzy rules base

In Table 1, based on the permutation and combination, it can be seen that there are 63 combinations of fuzzy values. Hence, on the basis of intuitive and expert considerations and then tuned by simulation tests, 63 if-then inferential rules are used here.

2.4.3 Fuzzy logic inference system

In order to meet the needs of practical work, the input and output of fuzzy logic inference system are both exact values. However, the operational objectives of fuzzy inference are fuzzy values. As a consequence, in order to transform the exact values into fuzzy values, we need to fuzzify the input values. Meanwhile, on the contrary, the output values of fuzzy inference need to be defuzzified for allocating the time resource during the target tracking process, which needs the exact values of ‘priority’. Hence, an integrated fuzzy logic inference system to calculate the priority of the targets is built in Fig. 3 [29].

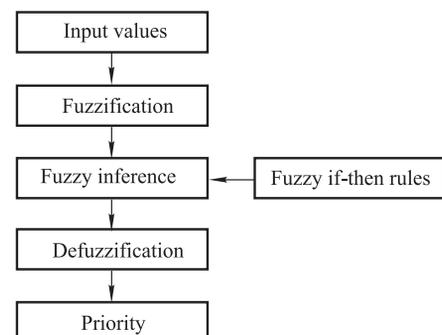


Fig. 3 Integrated fuzzy logic inference system

Through this system, the priority of targets can be generated jointly by the range, velocity and threat of targets.

3. Chance-constraint programming model

3.1 BCRLB

It is assumed that $\hat{\xi}_k^q$ is an estimation of state vector ξ_k^q . Hence, $\hat{\xi}_k^q$ is a function of the measurement value z_k^q . In the Bayesian estimation problem, the BCRLB C_{BCRLB} provides a low bound for the MSE in estimating the random vector ξ_k^q , and it is the inverse of BIM $J(\xi_k^q)$. The MSE of any estimator cannot be less than the BCRLB C_{BCRLB} [30]:

$$\mathcal{E}[(\hat{\xi}_k^q(z_k^q) - \xi_k^q)(\hat{\xi}_k^q(z_k^q) - \xi_k^q)^T] \geq C_{\text{BCRLB}}(\xi_k^q) = J^{-1}(\xi_k^q) \quad (17)$$

where $\mathcal{E}[\cdot]$ denotes expectation with respect to the joint probability density function (PDF) $p(z_k^q, \xi_k^q)$ of z_k^q and ξ_k^q . The matrix inequality means that

$$\mathcal{E}[(\hat{\xi}_k^q(z_k^q) - \xi_k^q)(\hat{\xi}_k^q(z_k^q) - \xi_k^q)^T] - C_{\text{BCRLB}}(\xi_k^q)$$

is a nonnegative definite matrix. The BIM $J(\xi_k^q)$ can be described as

$$J(\xi_k^q) = \mathcal{E} \left(\left(\frac{\partial \ln p(z_k^q, \xi_k^q)}{\partial \xi_k^q} \right) \left(\frac{\partial \ln p(z_k^q, \xi_k^q)}{\partial \xi_k^q} \right)^T \right). \quad (18)$$

The joint PDF $p(z_k^q, \xi_k^q)$ can be replaced by the product of PDF $p(\xi_k^q)$ and conditional PDF $p(z_k^q | \xi_k^q)$.

$$p(z_k^q, \xi_k^q) = p(\xi_k^q)p(z_k^q | \xi_k^q) \quad (19)$$

Hence, the BIM $J(\xi_k^q)$ can be divided into a prior information matrix $J_P(\xi_k^q)$ and a data information matrix $J_D(\xi_k^q)$ [30].

$$J(\xi_k^q) = J_P(\xi_k^q) + J_D(\xi_k^q) \quad (20)$$

The prior information $J_P(\xi_k^q)$ is determined by the motion equations of targets, and the beam illuminating time has no impact on it. On the contrary, the data information $J_D(\xi_k^q)$ is affected by the total illuminating time allocated to the targets. And the longer the radar illuminates the target, the larger the $J_D(\xi_k^q)$ is.

According to [30,31], the complete BIM $J(\xi_k^q)$ can be obtained.

$$J(\xi_k^q) = J_P(\xi_k^q) + J_D(\xi_k^q) = [Q_{k-1}^q + F_q J^{-1}(\xi_{k-1}^q) F_q^T]^{-1} + G_{\xi_k^q}^T R_{\xi_k^q}^{-1} G_{\xi_k^q} \Big|_{\xi_{k|k-1}^q} \quad (21)$$

where $G_{\xi_k^q}$ and $R_{\xi_k^q}$ denote the Jacobian matrix and the measurement covariance matrix evaluated at $\xi_{k|k-1}^q$, respectively. $\xi_{k|k-1}^q$ denotes the predicted state vector of the q th target for the case of zero process noise [32].

3.2 Establishment of CCP model based on fuzzy logic adaptive prioritization

Through the derivation of Section 3.1, the BCRLB $C_{\text{BCRLB}}(\xi_k^q)$ can be got as the inverse matrix of BIM $J(\xi_k^q)$. The diagonal elements of the BCRLB $C_{\text{BCRLB}}(\xi_k^q)$ denote the low bound of MSE of the state vector estimation. As shown in (21), the BCRLB $C_{\text{BCRLB}}(\xi_k^q)$ of the q th target can be predicted by recursive computation. Firstly, we pre-allocate the time resource over all the targets. Then, in conjunction with the predicted target positions, the data information matrix $J_D(\xi_k^q)$ can be deduced. Together with the BIM $J(\xi_{k-1}^q)$ of time $k-1$, the BIM $J(\xi_k^q)$ would be calculated, thus the BCRLB $C_{\text{BCRLB}}(\xi_k^q)$ would be also obtained. Based on the aforementioned, in order to build a resource allocation model conveniently and represent the tracking performance of each target accurately, the tracking BCRLB of the q th target can be represented through the square root of the sum of the elements on the leading diagonal:

$$F(T_k^q, \xi_k^q, h_k^q) = \sqrt{\text{trace}(C_{\text{BCRLB}}(T_k^q, \xi_k^q, h_k^q))} \quad (22)$$

where T_k^q denotes the dwell time of the q th target at the k th sample interval. h_k^q denotes the RCS of the q th target at the k th sample interval.

Herein, the tracking BCRLB of a single target is got. Suppose the priority of all the targets is the same. Then we can sum the tracking BCRLB of all the targets together for the total tracking BCRLB. In accordance with (21), the tracking BCRLB of the targets is related to many parameters. The dwell time vector T_k is concerned in this paper. In the actual tracking process, the total illuminating time, in which the beams illuminate the targets, is limited. In certain overload situations, to assure that the tasks can be accomplished as many as possible in the limited tracking time, the resource management model is built to minimize the total illuminating time conditioned on the specified total tracking error threshold. Therefore the conventional resource management model is got.

$$\begin{aligned} & \min \sum_{q=1}^Q T_k^q \\ & \text{s.t. } T_k^q \geq T_{\min} \\ & \sum_{q=1}^Q F(T_k^q, \xi_k^q, h_k^q) \leq \eta_0 \end{aligned} \quad (23)$$

where T_{\min} is the minimum of the dwell time of each target. η_0 is the specified total tracking error threshold.

Due to the difference of targets, the priority of targets is different. The priority can be reflected by the tracking BCRLB with different weight coefficients. Hence, in view of the priority of the targets, the resource management model can be reformulated as

$$\begin{aligned} & \min \sum_{q=1}^Q T_k^q \\ & \text{s.t. } T_k^q \geq T_{\min} \\ & \sum_{q=1}^Q [w_k^q \cdot F(T_k^q, \xi_k^q, h_k^q)] \leq \eta_0 \end{aligned} \quad (24)$$

where w_k^q is the weight coefficient of the q th target at the k th sample interval.

In practice, the target RCS is related to identification, attitude and position of the target, and also it is impacted by aspect angle, polarization and so on [13], i.e., the target RCS is unknown and uncertain. Consequently, the target RCS is regarded as a random variable in this paper. Then the deterministic resource allocation model cannot show the characteristic of the targets well and truly, and it cannot guarantee the robustness of the model either. In view of the above situation, the random CCP of the time resource management is introduced [33]. According to (24), the resource management model can be transformed into

$$\begin{aligned} & \min \sum_{q=1}^Q T_k^q \\ & \text{s.t. } T_k^q \geq T_{\min} \\ & \Pr \left\{ \sum_{q=1}^Q [w_k^q \cdot F(T_k^q, \xi_k^q, h_k^q)] \leq \eta_0 \right\} \geq \alpha. \end{aligned} \quad (25)$$

Because the coherent pulse is used in this paper, the dwell time T_k^q can be factorized as

$$T_k^q = L_k^q \cdot T_1. \quad (26)$$

The model (25) is equivalently transformed to

$$\begin{aligned} & \min \sum_{q=1}^Q L_k^q \\ & \text{s.t. } L_k^q \geq L_{\min} \\ & \Pr \left\{ \sum_{q=1}^Q [w_k^q \cdot F(L_k^q, \xi_k^q, h_k^q)] \leq \eta_0 \right\} \geq \alpha. \end{aligned} \quad (27)$$

The confidence level α in (25) and (27) is a probability at which it is desired that the stochastic constraint holds. Not only the identity, motion state, and number of the targets, but also the target environments and the amount of radar resources are the factors which impact the confidence level. Thus the selection of the confidence level is a result of synthesizing all kinds of factors.

As described at the beginning of Section 2, the number of targets is more than the number of beams. Hence, the targets should be allocated among the beams appropriately to ensure that the difference of illuminating time between all the beams is as small as possible. We can allocate the Q targets among the M beams like the following description.

Firstly, the dwell time of the Q targets is sorted from large to small. Then the top M elements of the sorted sequence are selected corresponding to the M beams. Thirdly, only the maximum element is selected from the remaining sequence each time to be added to the minimum time of the beams until the remaining elements are all allocated.

4. Theory and method for solving the model

In this section, we firstly describe the solving process of the fuzzy logic inference system detailedly. And then the hybrid intelligent optimization algorithm for solving the time resource CCP model is presented. Its object is to predict the optimal time resource allocation for next sample instant. Finally, we integrate the unscented Kalman filter (UKF) and the hybrid intelligent optimization algorithm to produce a target state estimation algorithm for the multiple target tracking.

4.1 Stochastic simulation

In order to verify whether the decision vector satisfies the confidence level, the stochastic simulation [33] for (27) is described as follows:

Step 1 Set $N' = 0$.

Step 2 Generate RCS vector $(\mathbf{h}_k)_i$ ($i = 1, 2, \dots, N$) of all the targets from their own probability space $(\Omega, \mathcal{A}, \text{Pr})_q$.

Step 3 If $\sum_{q=1}^Q [F(L_k^q, \xi_k^q, h_k^q)] \leq \eta_0$, then $N' \leftarrow N' + 1$.

Step 4 Repeat the second and third steps N times.

Step 5 $\text{Pr}(\mathbf{L}_k) = N'/N$.

Step 6 If $\text{Pr}(\mathbf{L}_k) \geq \alpha$, the decision vector \mathbf{L}_k satisfies the constraint condition; otherwise it does not.

4.2 Fuzzy logic inference system for calculating the priority

In the light of Fig. 3, the fuzzy logic inference system consists of four function modules: fuzzification, fuzzy infer-

ence, fuzzy if-then rules, and defuzzification. The solving method of each module would be elaborated [29,34,35].

4.2.1 Fuzzification

When the exact values are input, they should be fuzzified into the fuzzy values. In consequence, the essence of fuzzification is to transform the exact values into fuzzy values. The triangular fuzzifier is used to fuzzify the input values [35].

The triangular fuzzifier maps a real-value point $x^* \in U$ into a fuzzy set A' in U , which has the following triangular membership function:

$$\mu_{A'}(x) = \begin{cases} 1 - \frac{|x - x^*|}{\sigma}, & |x - x^*| \leq \sigma \\ 0, & \text{otherwise} \end{cases} \quad (28)$$

4.2.2 Fuzzy inference

Through the triangular fuzzifier, the exact values are changed to fuzzy values. The fuzzy if-then inference rules are given in Section 2.4.2. Then we can use multi-conditional fuzzy inference to compute the fuzzy value of the priority.

Suppose the number of fuzzy rules is N . Then the general schema of multi-conditional fuzzy inference is shown in Table 2.

Table 2 General schema of multi-conditional fuzzy inference

Rule number	Fuzzy rules
Rule 1	If $(A_1 \text{ AND } B_1 \text{ AND } C_1)$, then D_1 ;
Rule 2	If $(A_2 \text{ AND } B_2 \text{ AND } C_2)$, then D_2 ;
Rule 3	If $(A_3 \text{ AND } B_3 \text{ AND } C_3)$, then D_3 ;
\vdots	\vdots
Rule n	If $(A_N \text{ AND } B_N \text{ AND } C_N)$, then D_N ;
Fact	If $(A' \text{ AND } B' \text{ AND } C')$
Conclusion	then D'

In Table 2, A_i and A' are the fuzzy subsets of the universe X , B_i and B' are the fuzzy subsets of the universe Y , C_i and C' are the fuzzy subsets of the universe Z , and D_i and D' are the fuzzy subsets of the universe W ($i = 1, 2, \dots, N$).

It can be seen that these rules of Table 2 are in the form of "If... then..." statements. Each individual rule could be represented as

$$R_i = A_i \text{ AND } B_i \text{ AND } C_i \rightarrow D_i \quad (29)$$

where R_i denotes the fuzzy relation.

According to Mamdani inference [34], we use Mamdani's product implication $A \wedge B$ for $A \rightarrow B$, where \wedge denotes the minimum operator. According to (29), the fuzzy relation μ_{R_i} of each rule i could be represented as

$$\mu_{R_i}(x, y, z, w) =$$

$$[\mu_{A_i}(x) \wedge \mu_{B_i}(y) \wedge \mu_{C_i}(z)] \wedge \mu_{D_i}(w) \quad (30)$$

where μ denotes the membership function, and $x \in X$, $y \in Y$, $z \in Z$, $w \in W$.

The overall protocol is then a relation R formed by 'OR-ing' together with the R_i 's:

$$R = \bigcup_{i=1,2,\dots,N} R_i \quad (31)$$

Then the conclusion D' can be described as

$$\begin{aligned} D' &= (A' \text{ AND } B' \text{ AND } C') \cap R = \\ &= (A' \text{ AND } B' \text{ AND } C') \cap \left(\bigcup_{i=1,2,\dots,N} R_i \right) = \\ &= D'_1 \cup D'_2 \cup \dots \cup D'_N \end{aligned} \quad (32)$$

where \cap is the standard fuzzy intersection.

$$\begin{aligned} D'_i &= (A' \text{ AND } B' \text{ AND } C') \cap \\ &= [(A_i \text{ AND } B_i \text{ AND } C_i) \rightarrow D_i]. \end{aligned} \quad (33)$$

And the membership function is

$$\begin{aligned} \mu_{D'_i}(w) &= [\mu_{A'}(x) \wedge \mu_{A_i}(x)] \wedge \\ &= [\mu_{B'}(y) \wedge \mu_{B_i}(y)] \wedge \\ &= [\mu_{C'}(z) \wedge \mu_{C_i}(z)] \wedge \mu_{D_i}(w) = \gamma_i \wedge \mu_{D_i}(w) \end{aligned} \quad (34)$$

where γ_i represents the minimum of the degrees to which the antecedents A_i , B_i and C_i are respectively compatible with the given fact A' , B' and C' .

The geometrical significance of fuzzy inference is that the conclusion D' is got by truncating each set D_i by the value of γ_i and taking the union of the truncated sets.

4.2.3 Defuzzification

Due to the plausibility, computational simplicity, and continuity, the center average defuzzifier is used here for defuzzification [35]. The fuzzy set D' is the union of N fuzzy sets. Let \bar{w}_i be the center of the i th fuzzy set and $\mu_{\max}^i(w)$ be its maximal value of the membership function. The center average defuzzifier determines w^* as

$$w^* = \frac{\sum_{i=1}^N [\bar{w}_i \mu_{\max}^i(w)]}{\sum_{i=1}^N \mu_{\max}^i(w)} \quad (35)$$

4.2.4 Fuzzy logic inference system

The integrated fuzzy logic inference system has been displayed in Section 2.4.3. Through this system, we can get

the exact value of the priority according to the exact values of the range, velocity and threat.

4.3 Hybrid intelligent optimization algorithm

Because the target RCS is considered as a random variable, the stochastic simulation is introduced and embedded into GA to constitute a hybrid intelligent optimization algorithm for solving the random CCP model. Hence at time k , we can predict the optimal time resource allocation $T_{k+1,opt}$ of time $k+1$. The steps are as follows:

Step 1 According to the motion equation $\xi_{k+1|k}^q = F_q \cdot \xi_k^q$ with a zero process noise, predict the state vector $\xi_{k+1|k}^q$ of time $k+1$.

Step 2 Calculate the priority vector w_{k+1} of all the targets by fuzzy logic inference system, and then get the complete time resource management model.

Step 3 Initialize the population, and check the feasibility of the generated chromosomes with the stochastic simulation.

Step 4 Update the chromosomes by crossover and mutation operations, and check the feasibility of the updated chromosomes with the stochastic simulation, and if they do not satisfy the constraint, correct the chromosomes.

Step 5 Calculate the objective function values of all the chromosomes, and then compute the fitness of each chromosome according to the objective function values

Step 6 Select the chromosomes by spinning the roulette wheel.

Step 7 Repeat the Steps 4–6 for a given number of cycles.

Step 8 Return the best chromosome as the optimal time allocation $T_{k+1,opt}$.

4.4 Target state estimation algorithm

Based on the aforementioned solving process, in conjunction with UKF, the target state estimation algorithm for multiple target tracking is obtained. The complete procedure is described as follows:

Step 1 Let $k=1$, $T_{k,opt} = T_0$ (T_0 denotes initial time allocation according to target detection), and for the q th target, initialize $\xi_{k-1|k-1}^q$, the covariance $P_{k-1|k-1}^q = J^{-1}(\xi_{k-1|k-1}^q)$.

Step 2 Illuminate all the targets in line with $T_{k,opt}$. Then get the measurement value z_k^q of each target and calculate $R_{\xi_k^q}$ according to (13).

Step 3 Compute the sigma points $\chi_{i,k-1|k-1}^q$ and their

weights $\omega_{i,k}$ in accordance with the following equations:

$$\begin{cases} \chi_{0,k-1|k-1}^q = \xi_{k-1|k-1}^q \\ \chi_{i,k-1|k-1}^q = \xi_{k-1|k-1}^q + \frac{(\sqrt{(I+\varsigma)P_{k-1|k-1}^q})_i}{\sqrt{I+\varsigma}}, \quad i=1,2,\dots,I \\ \chi_{i,k-1|k-1}^q = \xi_{k-1|k-1}^q - \frac{(\sqrt{(I+\varsigma)P_{k-1|k-1}^q})_{i-I}}{\sqrt{I+\varsigma}}, \quad i=I+1,I+2,\dots,2I \end{cases} \quad (36)$$

$$\begin{cases} \omega_{0,k} = \frac{\varsigma}{I+\varsigma} \\ \omega_{i,k} = \frac{1}{2(I+\varsigma)}, \quad i=1,2,\dots,2I \end{cases} \quad (37)$$

where ς is a scaling parameter, and $(\sqrt{(I+\varsigma)P_{k-1|k-1}^q})_i$ is the i th row or column of the matrix square root, I is the dimension of the state vector, and $\omega_{i,k}$ is the weight that is associated with the i th point.

Step 4 Transform each sigma point through the motion equation, and calculate the mean $\xi_{k|k-1}^q$ and covariance $P_{k|k-1}^q$:

$$\begin{cases} \chi_{i,k|k-1}^q = F_q \cdot \chi_{i,k-1|k-1}^q \\ \xi_{k|k-1}^q = \sum_{i=0}^{2I} (\omega_i \cdot \chi_{i,k|k-1}^q) \\ P_{k|k-1}^q = \sum_{i=0}^{2I} \omega_i (\chi_{i,k|k-1}^q - \xi_{k|k-1}^q) \cdot (\chi_{i,k|k-1}^q - \xi_{k|k-1}^q)^T + Q_{k-1}^q \end{cases} \quad (38)$$

Step 5 Transform each sigma point through the measurement equation, and compute the mean $z_{k|k-1}^q$ and covariances $P_{zz,k}^q$ and $P_{xz,k}^q$:

$$\begin{cases} z_{i,k|k-1}^q = g(\chi_{i,k|k-1}^q) \\ z_{k|k-1}^q = \sum_{i=0}^{2I} \omega_i \cdot z_{i,k|k-1}^q \\ P_{zz,k}^q = \sum_{i=0}^{2I} \omega_i (z_{i,k|k-1}^q - z_{k|k-1}^q) (z_{i,k|k-1}^q - z_{k|k-1}^q)^T + R_{\xi_k^q} \\ P_{xz,k}^q = \sum_{i=0}^{2I} \omega_i (\chi_{i,k|k-1}^q - \xi_{k|k-1}^q) (z_{i,k|k-1}^q - z_{k|k-1}^q)^T \end{cases} \quad (39)$$

Step 6 Calculate the gain matrix K_k^q , and update the state vector $\xi_{k|k}^q$ and covariance matrix $P_{k|k}^q$.

$$\begin{cases} K_k^q = P_{xz,k}^q \cdot (P_{zz,k}^q)^{-1} \\ \xi_{k|k}^q = \xi_{k|k-1}^q + K_k^q \cdot (z_k^q - z_{k|k-1}^q) \\ P_{k|k}^q = P_{k|k-1}^q - K_k^q \cdot P_{zz,k}^q \cdot (K_k^q)^T \end{cases} \quad (40)$$

Step 7 According to the hybrid intelligent optimization algorithm, predict the optimal time resource allocation $T_{k+1,opt}$ of time $k+1$.

Step 8 Let $k = k + 1$, and go to Step 2.

5. Simulation result and analysis

In order to verify the validity of the proposed algorithm, some numerical simulation results are provided in this section. The parameters configuration is as follows.

Suppose the OAR is located at (0,0) km, and three beams with the same transmitting power are generated simultaneously for tracking the targets. The effective bandwidth of the transmitting signal is $B_k^q = 5$ MHz, and the effective time duration of each coherent pulse is $T_1 = 0.03$ ms. The carrier frequency of each beam is $f_c = 10$ GHz, and the wavelength is 0.03 m. The sample interval of the tracking process is $T_0 = 3$ s, and we use 40 frames for this simulation.

The RCS of each target is viewed as a random variable, i.e., the RCS obeys a stochastic distribution. Without loss of generality, it is assumed that all the targets have the same PDF of RCS. We adopt the chi-square distribution of four degrees of freedom with mean 2.151 7 [36] in Fig. 4.

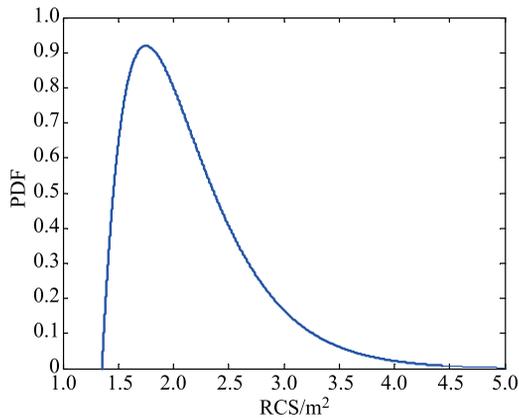


Fig. 4 PDF of $|h_q|$

There are $Q = 9$ targets with the following parameters in Table 3.

Table 3 Parameters of all the targets

Target	Position/km	Distance/km	Velocity/(m/s)
1	(-100,60)	116.62	(86,-51)
2	(-90,90)	127.28	(354,-354)
3	(-80,120)	144.22	(444,-666)
4	(-60,100)	116.62	(-51,86)
5	(0,110)	110	(0,-600)
6	(60,92)	109.84	(164,251)
7	(90,104)	137.54	(-458,-529)
8	(120,98)	154.93	(-697,-569)
9	(120,47)	128.88	(-186,-73)

The deployment of the targets and OAR can be seen in Fig. 5.

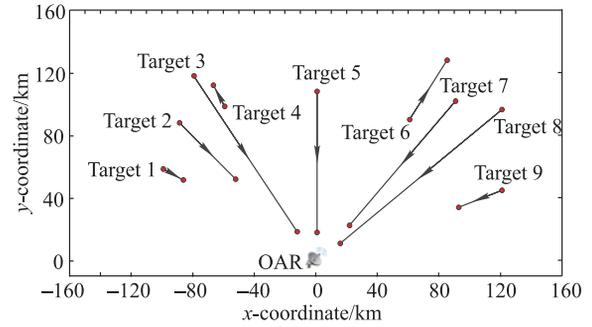


Fig. 5 Deployment of the targets and OAR

To emphasize and highlight the advantages of the resource allocation CCP, we firstly discuss and analyze the time resource CCP without the fuzzy logic priority in Situation 1. Under the condition of the same tracking error threshold, the total time for illuminating all the targets subject to different confidence levels is calculated. Then the impacts of fuzzy logic priority embedded into CCP on the time resource management of multiple target tracking are studied in Situation 2.

5.1 Situation 1

Due to the randomness of target RCS, the CCP can be used to balance the system resource and tracking accuracy. In other words, the probability of the RCS $|h_q|$ appearing around the interval endpoints is very low, so the resource programming does not need to satisfy the constraint completely, but the probability of the constraint holding is no less than a certain confidence level. As a result of this programming, large amounts of time resource will be cut down because of abandoning the extreme case that the constraint is satisfied in a low confidence level. Suppose the given total tracking error threshold is described in Fig. 6 as time goes on.

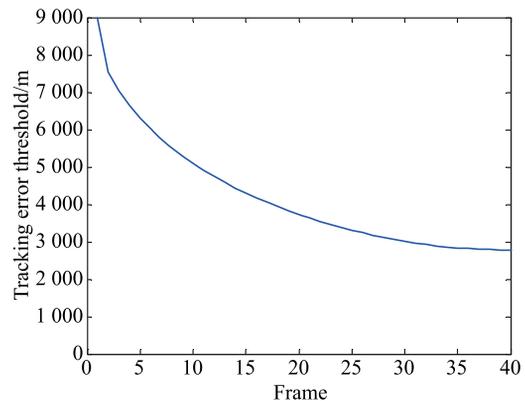


Fig. 6 Specified tracking error threshold

We set the confidence levels to 0.99, 0.95 and 0.9, respectively. The total illuminating time of each frame is nor-

malized by the total system time T_S .

$$\sigma = \sum_{q=1}^Q T_k^q / T_S = \sum_{q=1}^Q L_k^q / L_S \quad (41)$$

where σ is the time resource saving rate, and L_S is the pulse number corresponding to T_S .

On the condition that the specified confidence level is satisfied, the total illuminating time and the illuminating time of each beam can be obtained in Fig. 7 and Fig. 8, respectively.

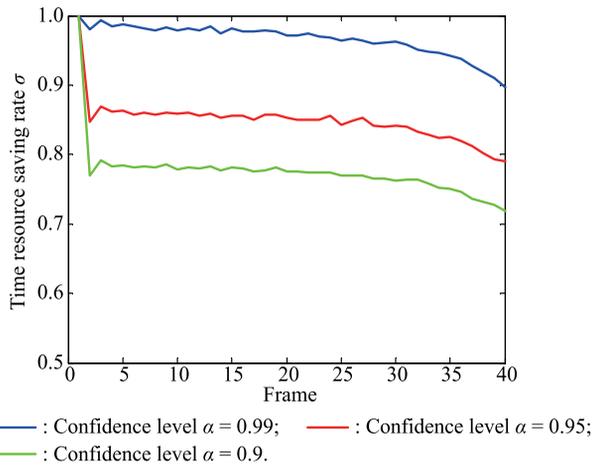


Fig. 7 Time resource saving rate of each frame

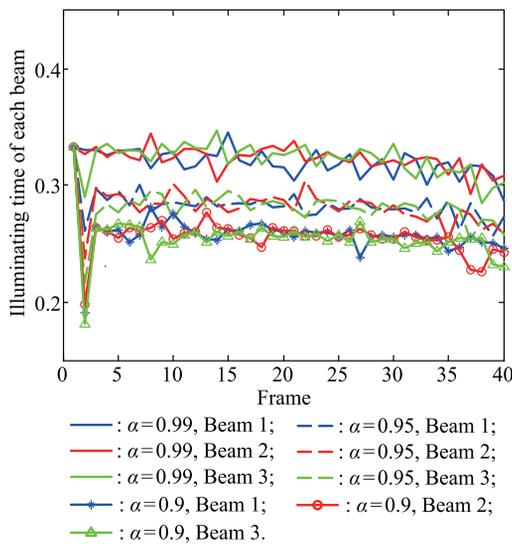


Fig. 8 Illuminating time of each beam

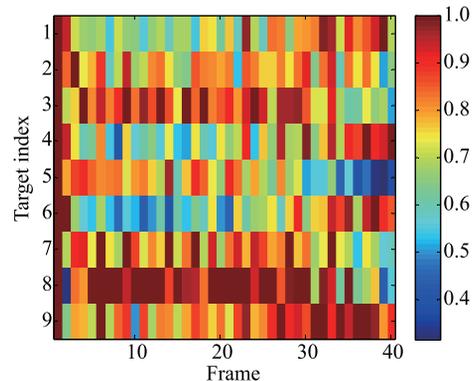
As can be seen in Fig. 7, the total illuminating time to all the targets is reduced following the decrease of the confidence level. When the confidence level is 0.9, the total illuminating time is brought down by about 22%. As can be also found through observation, though the tracking error threshold declines over time, the illuminating time

is reducing slowly all the time instead of remaining unchanged. That is because the illuminating time for keeping the tracking error threshold decreases with the targets approaching OAR. When the tracking error threshold levels off between 35–40 frames, the illuminating time starts to decline rapidly. The illuminating time saving rate is relative to the distribution function of target RCS.

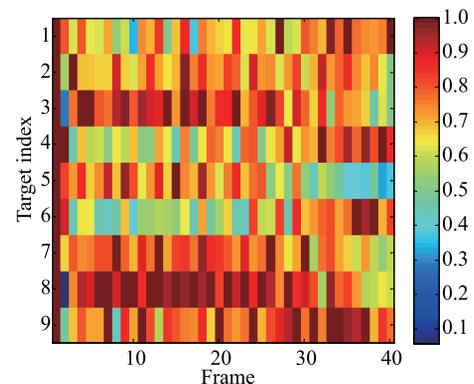
In Fig. 8, the illuminating time of each beam under different confidence level is described. The illuminating time lessens in the wake of the decrease of the confidence level. Through the rational allocation of targets among the three beams, the illuminating time of the three beams is approximately equal.

Besides saving large time resource, the resource programming algorithm can also allocate the dwell time intelligently. The dwell time of each target is normalized by the maximum dwell time of all the targets at each frame. The dwell time allocated to each target can be shown in Fig. 9.

In Fig. 9, we can see that the target 3 and target 8 take up the most time at the beginning, and meanwhile, the target 4 and target 6 occupy the least time. The reason is that target 3 and target 8 are the farthest two, and target 4 and target 6 are the closest two at the initial time.



(a) $\alpha=0.99$



(b) $\alpha=0.95$

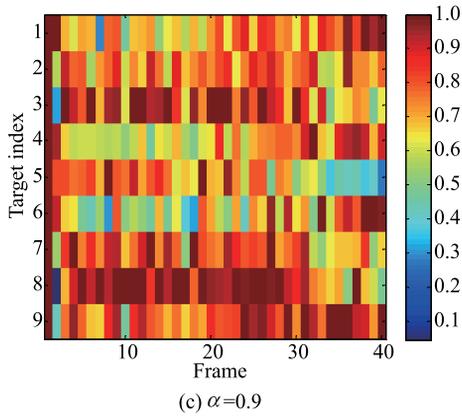


Fig. 9 Dwell time of each target under different confidence levels

Therefore, in order to satisfy the tracking error threshold, the dwell time allocated to target 3 and target 8 is more than the dwell time allocated to target 4 and target 6 without considering the target priority. However, as time goes by, target 3 and target 8 become the closest two, and target 4 and target 6 become the farthest two. Then the dwell time allocated to target 3 and target 8 decreases, and the dwell time allocated to target 4 and target 6 increases.

5.2 Situation 2

The simulation and analysis in Situation 1 ignores the priority of targets, however, as a matter of fact, the priority of targets is very important to the resource allocation of radar system. Consequently, the time resource allocation in conjunction with the priority is considered in Situation 2. The simulation parameters are the same as Situation 1. The fuzzy logic inference method is embedded into the CCP model for total illuminating time allocation. The priorities of the targets are shown in Fig. 10.

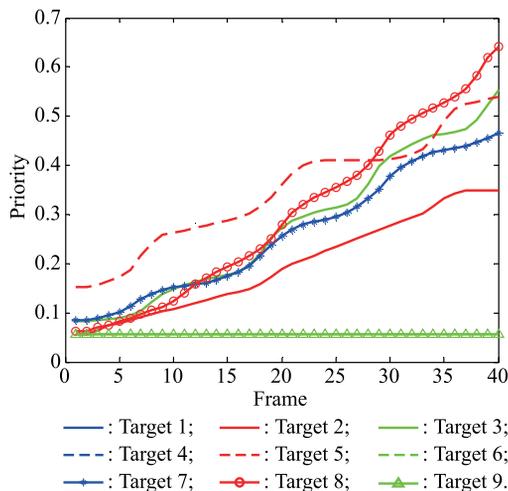


Fig. 10 Priority of the targets over time

The priority integrates the range, velocity and degree of threat. As shown in Fig. 10, the priority of each target

varies continuously [20]. Hence, the changes of the targets can be reflected by priority. In regard to target 1 and target 9, the priority is very low and changes little as time goes on for the farther distance, slower velocity and lower threat. Similar to target 1 and target 9, the priority is very low since target 4 and target 6 are flying away from the OAR all the time. At the initial time of the tracking, target 5 has the maximum dwell time for the highest priority, however, target 3 and target 8 approach the radar with higher velocity, so the priorities of target 3 and target 8 become the highest two gradually and the radar illuminates them with the longest time.

When the confidence level is 0.9, the total illuminating time is shown in Fig. 11 while the priority is and is not taken into account. The total illuminating time is cut down strikingly for the priority. As time goes on, the differences of the range, velocity and threat are becoming bigger and bigger. Therefore, there is no need to spend much time on the targets with low priority. The targets with high priority are always approaching the OAR. Hence, the dwell time to the targets for keeping the tracking error small is not too long.

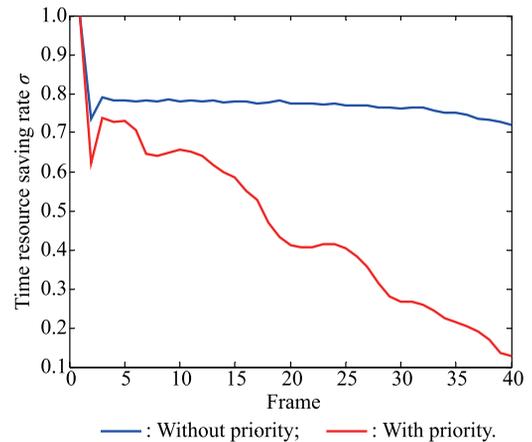


Fig. 11 Total illuminating time of all the targets

In Situation 1, all the targets have the same priority. As a consequence, the weight coefficients of the targets in (27) are all 1, i.e., $w_k^q = 1$. In analogy with Situation 1, the weight coefficients in Situation 2 can be expressed in the following equation:

$$w_k^q = Q \cdot \rho_k^q / \sum_{k=1}^Q \rho_k^q \tag{42}$$

where ρ_k^q denotes the priority. The larger the weight coefficient is, the longer the illuminating time is, so the higher the tracking accuracy is.

Fig. 12 illustrates the proportion of the illuminating time of each target. In Fig. 12(a), although the resource allocation is affected by the targets moving, compared with

Fig. 12(b), the effect is so slight that the contrast of the dwell time on the targets is inconspicuous. However, in Fig. 12(b), when we calculate the priority of targets through fuzzy logic inference system, not only the total illuminating time is economized strikingly, but also the dwell time on each target is allocated reasonably and effectively.

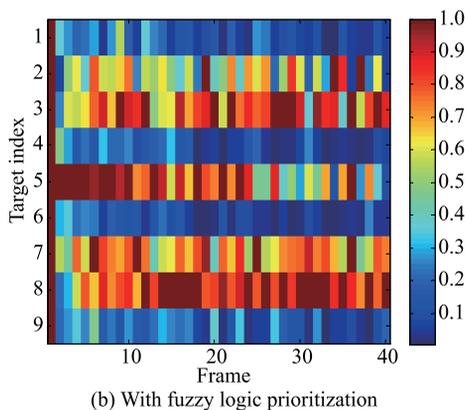
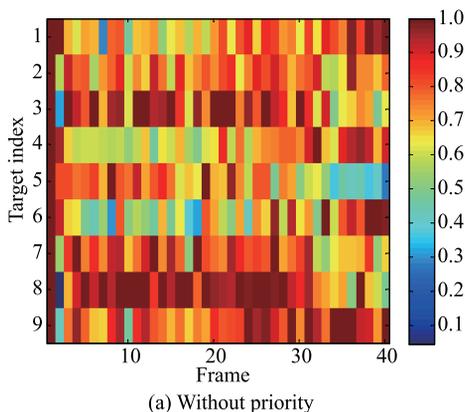


Fig. 12 Illuminating time of each target

In Fig. 13, the target indices of the longest dwell time are listed. In Fig. 13(a), when the priority is not considered, the target indices with the longest dwell time are chaotic. For instance, target 1, target 4, target 6 and target 9 obtain the longest dwell time at certain frames unexpectedly.

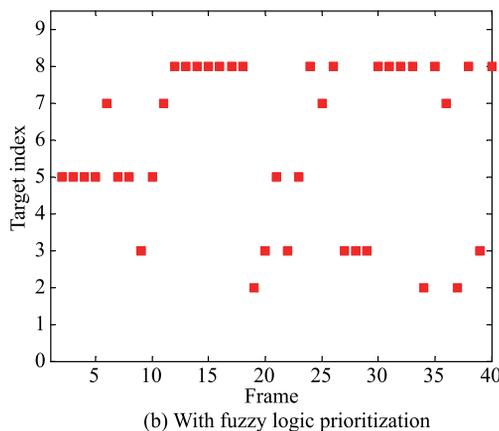
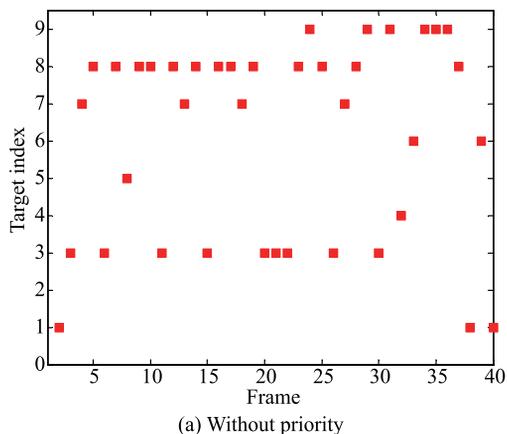


Fig. 13 Target indices with the longest illuminating time at each frame

In Fig. 13(b), the target indices with the longest dwell time concentrate upon target 2, target 3, target 5, target 7 and target 8 for the high priority. More resources allocated to the closer, the faster and the more threatening targets are logical.

The dwell time on the targets with low priority is short and the dwell time on the targets with high priority is long. Hence, compared with Fig. 14(a), the tracking error of the targets with high priority gets smaller in Fig. 14(b).

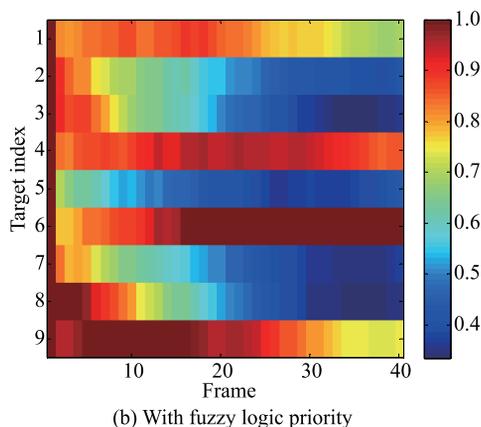
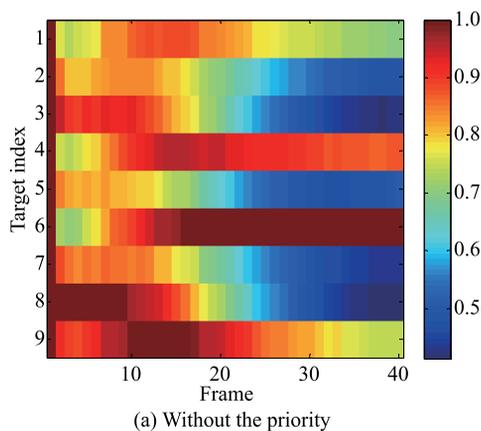


Fig. 14 Tracking error of each target

6. Conclusions and future work

This paper proposes a time resource management scheme based on CCP in conjunction with fuzzy logic priority for multiple target tracking of OAR. The aim of this scheme is to minimize the total illuminating time conditioned on the specified confidence level. The RCS of each target is considered as a random variable, and the desired total tracking performance of the targets is deemed as the constraint. The target priority, which is computed through adaptive fuzzy logic inference system, is embedded into the hybrid intelligent optimization algorithm, which integrates stochastic simulation and GA, to calculate the optimal dwell time allocation of next frame, and then the predicted value is applied to UKF to constitute the target state estimation algorithm for solving the multiple target tracking. As seen from Situation 1, compared with the traditional deterministic resource allocation model, the CCP model can not only assure the stability of the model, but also reduce the illuminating time obviously conditioned on the confidence level. As the confidence levels decrease, the saving time resource increases. In Situation 2, considering the target priority together with CCP, the total illuminating time can be brought down further. Moreover, the illuminating time could be allocated more reasonably over the targets. Thereby, more time resources would be saved to accomplish other tasks.

The future work will be directed to the following three aspects:

(i) The scenario of multiple target tracking in this paper is a little simple. In practical process of multiple target tracking, the target loss is a common occurrence. We need to allow for the resource management scheme when the target loss happens.

(ii) The time resource management of this paper focusing on multiple target tracking is partial. Hence, the time resource allocation of joint detection and tracking should be studied. The work of this paper lays the foundation for the time resource allocation of joint detection and tracking.

(iii) The power resource is a kind of important resource in radar system. Thus the study of joint power and the time resource management algorithm is necessary.

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